

**Percent:** The decimal number times 100 .

Ex:  $0.25 = 25\%$  ,  $7.431 = 743.1\%$  ,  $629.73\% = 6.2973$  ,  $0.1\% = 0.001$  .

**Negative Integer Exponents:** Any number written with a **negative exponent** means the reciprocal of that number to the positive exponent.

Ex:  $17^{-31} = \frac{1}{17^{31}}$  .

**Scientific Notation:** Any decimal number can always be written as a non-zero integer followed by a decimal point followed by the rest of the number, all multiplied by some power of 10.

Ex:  $4,723.5 = 4.7235 \times 10^3$  ,  $0.001496 = 1.496 \times 10^{-3}$  ,  $0.00000007214 = 7.214 \times 10^{-8}$  ,  
 $5,120,000 = 5.12 \times 10^6$  .

This is an easy way to write very large or very small numbers. The only tricky part is to figure out the correct power of 10. **The magnitude of the power of 10 equals the number of places the decimal point is moved.** The sign of the power of 10 is determined by whether the magnitude of the original number is larger than 1 or smaller than 1 (remember that  $10^{-anything} < 1$  while  $10^{anything} > 1$  for (*anything*)  $> 0$ ).

The real value of scientific notation lies in the use of the rules of exponents to manipulate numbers.

Ex:

$$\sqrt{400,000,000} \cdot (0.000000027)^{1/3} = (4 \times 10^8)^{1/2} \cdot (27 \times 10^{-9})^{1/3} = (2 \times 10^4)(3 \times 10^{-3}) = 2 \cdot 3 \times 10^{4-3} = 6 \times 10 = 60$$

**Prime Decomposition:** Every integer can be written as a product of prime numbers. There is only one way that this can be done.

Ex:  $342 = 2 \cdot 171 = 2 \cdot 9 \cdot 19 = 2 \cdot 3^2 \cdot 19$  , which is the prime decomposition of 342 .

**Testing For Primes:** When trying to determine if some number, call it N, is a prime you only have to check for prime factors up to  $\sqrt{N}$  .

Ex: Is 119 prime?

Soln: Since  $11 \cdot 11 = 121$  you only have to check for prime factors less than 11.

2 and 5 are not factors by inspection.

Adding the digits gives 11 so 3 is not a factor.

The only prime left less than 11 is 7.  $119/7 = 17$  so the answer is NO.

**Relative Primes:** Two numbers which have no prime factors in common are **relatively prime**.

Ex: Which of the three pairs of numbers are relatively prime: (342,195), (95,114), (990,323) ?

Soln:  $3 + 4 + 2 = 9$  ,  $1 + 9 + 5 = 15$  and both sums are divisible by 3, so 3 must be a common factor of the first pair, so 342 and 195 are NOT relatively prime.

$95 = 5 \cdot 19$  , and 5 is not a factor of 114 , so try 19.  $114/19 = 6$  , so 19 is a common factor of the second pair, so 95 and 114 are NOT relatively prime.

$990 = 10 \cdot 99 = 10 \cdot 9 \cdot 11 = 2 \cdot 3^2 \cdot 5 \cdot 11$  , so see if these primes are factors of 323.

Not 2 or 5, adding digits gives 8 so not 3,  $3 - 2 + 3 = 4$  so not 11. None of the factors of 990 is a factor of 323, so 990 and 323 ARE relatively prime.

(Notice that since  $323 = 17 \cdot 19$  neither 990 nor 323 are prime numbers.)

**Numbers 3 Homework Problems****(NO CALCULATORS)**

- a) Express  $62\frac{1}{2}\%$  as a common fraction in lowest terms.
- b) Express  $16\frac{2}{3}\%$  as a common fraction in lowest terms.
- c) Write the decimal equivalent to  $\frac{3}{5}\%$  .
- d) Write the common fraction equivalent to  $20\frac{5}{6}\%$  .
- e) Write  $62\frac{2}{3}\%$  as a common fraction.
- f) Write  $22\frac{1}{2}\%$  as a common fraction.
- g) Express  $6\frac{1}{4}\%$  as a common fraction.
- h) Write the common fraction equivalent to  $71\frac{3}{7}\%$  .
- i) 24 is what percent of 73 ? Express your answer to the nearest tenth of a percent.
- j) Find the absolute value of the difference between the two largest of the following numbers. Express your answer as a decimal. (a)  $\frac{3}{8}$ , (b) 0.3, (c) 35%, (d)  $\frac{1}{3}$  .
- k) What is  $(0.00000003)(1,700,000,000)$  ?
- l) What is  $\frac{(80,000,000)^2(0.000003)}{(600,000)(0.0002)^4}$  ?
- m) Which pair(s) are relatively prime: (a) (23,115) , (b) (72,35) , (c) (256,27) , (d) (990,637)